# Optimal plot size in single or intercropping sorghum and showy rattlebox 

Alberto Cargnelutti Filho ${ }^{* *}$ © , Ismael Mario Márcio Neu ${ }^{1}$ © , Vinicius Severo Trivisiol ${ }^{1}{ }^{\oplus}$, Lucas Fillipin Osmari¹0, Vithória Morena Ortiz¹ ${ }^{\text {© }}$<br>${ }^{1}$ Universidade Federal de Santa Maria, Santa Maria, RS, Brasil, E-mail: alberto.cargnelutti.filho@gmail.com; ismaelmmneu@hotmail.com; vinicius trivisiol@hotmail.com; lucasfosmari@gmail.com; vithoria.ortiz159@gmail.com

ABSTRACT: The objective of this study was to determine the optimal plot size to evaluate fresh matter productivity of sorghum (Sorghum bicolor (L.) Moench) and showy rattlebox (Crotalaria spectabilis Roth.). Fifteen uniformity trials (blank experiments) with sorghum and showy rattlebox, in single or intercropping, were carried out. The fresh matter productivity was evaluated in 540 basic experimental units (BEU) of $1 \times 1 \mathrm{~m}$ ( 15 trials $\times 36 \mathrm{BEU}$ per trial). The plot size was determined by the method of Hatheway (1961), in scenarios formed by combinations of treatment numbers, repetitions numbers, and levels of experimental precision. To evaluate the fresh matter productivity of sorghum and showy rattlebox, in single or intercropping, with 5 to 30 treatments and with five repetitions, plots of $10 \mathrm{~m}^{2}$ of useful area are sufficient for differences between treatments of $24 \%$ of the overall average of the experiment to be considered significant at 0.05 probability.

Key words: Crotalaria spectabilis Roth.; experimental dimensions; soil cover crop; Sorghum bicolor (L.) Moench.

## Tamanho ótimo de parcela em cultivo solteiro e consorciado de sorgo e crotalária spectabilis

RESUMO: O objetivo deste trabalho foi determinar o tamanho ótimo de parcela para avaliar a produtividade de matéria fresca de sorgo (Sorghum bicolor (L.) Moench) e crotalária spectabilis (Crotalaria spectabilis Roth.). Foram realizados quinze ensaios de uniformidade (experimentos em branco) com sorgo e crotalária spectabilis, em cultivo solteiro e consorciado. Foi avaliada a produtividade de matéria fresca em 540 unidades experimentais básicas (UEB) de $1 \times 1 \mathrm{~m}$ (15 ensaios $\times 36$ UEB por ensaio). Foi determinado o tamanho de parcela, por meio do método de Hatheway (1961), em cenários formados por combinações de números de tratamentos, números de repetições e níveis de precisão experimental. Para avaliar a produtividade de matéria fresca de sorgo e crotalária spectabilis, em cultivo solteiro ou consorciado, com 5 a 30 tratamentos e com cinco repetições, parcelas de $10 \mathrm{~m}^{2}$ de área útil são suficientes para que diferenças entre tratamentos de $24 \%$ da média geral do experimento sejam consideradas significativas a 0,05 de probabilidade.

Palavras-chave: Crotalaria spectabilis Roth.; dimensionamentos experimentais; cultura de cobertura de solo; Sorghum bicolor (L.) Moench.

[^0]
## Introduction

Sorghum (Sorghum bicolor (L.) Moench) and showy rattlebox (Crotalaria spectabilis Roth.) have been evaluated for phytomass production (Pereira et al., 2012; Torres et al., 2014; Santos et al., 2020), the interference of these species on corn and bean grain yields (Torres et al., 2014), and on soil chemical and physical attributes (Passos et al., 2017). In these surveys, the number of treatments evaluated ranged from six to fifteen. Four repetitions and plots of $37.5 \mathrm{~m}^{2}$ (Pereira et al., 2012), $63 \mathrm{~m}^{2}$ (Torres et al., 2014), and $50 \mathrm{~m}^{2}$ (Passos et al., 2017) were used. However, the criteria used to define the plot size were not mentioned.

The plot size should be properly sized in order to minimize experimental error and, consequently, increase the accuracy of inferences regarding the treatments evaluated. Uniformity trials (blank experiments), that is, without treatments, make it possible to generate data for sizing in future experiments.

Methodologies from Smith (1938) and Hatheway (1961) can be applied to calculate the optimal plot size according to the number of treatments, number of repetitions, and experimental precision. These methodologies have been used in grain sorghum (Lopes et al., 2005; Brum et al., 2008), sunflower (Sousa et al., 2016), banana (Donato et al., 2018), forage palm (Guimarães et al., 2020), buckwheat (Cargnelutti Filho et al., 2020a), and tomato (Oliveira et al., 2021). It has still been used, in single and intercropped cultivation of black oat + vetch (Cargnelutti Filho et al., 2020b), millet + slender leaf rattlebox (Cargnelutti Filho et al., 2021a), millet + showy rattlebox (Cargnelutti Filho et al., 2021b), and intercropping of black oat + common vetch + forage turnip (Cargnelutti Filho et al., 2022).

Thus, the objective of this study was to determine the optimal plot size to evaluate the fresh matter productivity of sorghum (S. bicolor (L.) Moench) and showy rattlebox (C. spectabilis Roth.) in scenarios formed by combinations of treatment numbers, repetitions numbers, and levels of experimental precision.

## Materials and Methods

Fifteen uniformity trials with sorghum (S. bicolor (L.) Moench) cultivar Nutribem ( S ) and showy rattlebox ( $C$. spectabilis Roth.) (CS), were conducted in an experimental area located at $29^{\circ} 42^{\prime} \mathrm{S}, 53^{\circ} 49^{\prime} \mathrm{W}$, and 95 m of altitude. The climate at this site is Cfa humid subtropical, according to the Köppen-Geiger classification, with hot summers and no dry season (Alvares et al., 2013). The soil is Arenic Dystrophic Red Argissolo (Santos et al., 2018).

The following compositions of sowing densities of $S$ and CS crops were arranged: $100 \%$ of $\mathrm{S}\left(15 \mathrm{~kg} \mathrm{ha}^{-1}\right) ; 75 \%$ of $\mathrm{S}\left(11.25 \mathrm{~kg} \mathrm{ha}{ }^{-1}\right)+25 \%$ of CS ( $\left.5.625 \mathrm{~kg} \mathrm{ha}^{-1}\right) ; 50 \%$ of $\mathrm{S}(7.5$ $\left.\mathrm{kg} \mathrm{ha}{ }^{-1}\right)+50 \%$ of CS (11.25 kg ha ${ }^{-1}$ ); $25 \%$ of S ( $3.75 \mathrm{~kg} \mathrm{ha}^{-1}$ ) + $75 \%$ of CS (16.875 kg ha ${ }^{-1}$ ); and $100 \%$ of CS ( $22.5 \mathrm{~kg} \mathrm{ha}^{-1}$ ). For each composition, three uniformity trials (repetitions) were conducted. On October 28, 2020, in all trials, $35 \mathrm{~kg} \mathrm{ha}^{-1}$ of N ,
$135 \mathrm{~kg} \mathrm{ha}^{-1}$ of $\mathrm{P}_{2} \mathrm{O}_{5}$, and $135 \mathrm{~kg} \mathrm{ha}^{-1}$ of $\mathrm{K}_{2} \mathrm{O}$ were incorporated into the soil, and then sowing was carried out by broadcast.

In each uniformity trial, a $6 \times 6 \mathrm{~m}\left(36 \mathrm{~m}^{2}\right)$ area was demarcated. This area was divided into 36 basic experimental units (BEU) of $1 \times 1 \mathrm{~m}\left(1 \mathrm{~m}^{2}\right)$, forming a matrix of six rows and six columns. At 79 days after sowing, when the sorghum plants were in flowering (reproductive stage) and the showy rattlebox plants in the vegetative stage, fresh matter (FM) productivity was evaluated. For this, in each BEU, the plants were cut near the soil surface and then the fresh matter was weighed on a digital scale (accuracy: 1 g ), obtaining the FM in $\mathrm{g} \mathrm{m}^{-2}$.

With FM data from the 36 BEU , plots with $\mathrm{X}_{\mathrm{R}} \mathrm{BEU}$ adjacent in the row and $X_{c} B E U$ adjacent in the column were planned. The plots with distinct sizes and/or shapes were planned as $\left(X=X_{R} \times X_{C}\right)$, i.e., $(1 \times 1),(1 \times 2),(1 \times 3),(1 \times 6),(2 \times 1),(2 \times 2),(2 \times 3)$, $(2 \times 6),(3 \times 1),(3 \times 2),(3 \times 3),(3 \times 6),(6 \times 1),(6 \times 2)$, and $(6 \times 3)$. The abbreviations $X_{R}, X_{C^{\prime}}$, and $X$, stand for number of adjacent BEU in the row, number of adjacent BEU in the column, and plot size in number of BEU, respectively.

For each plot size $(X)$ were determined: $n$ - number of plots with X BEU size $(n=36 / X)$; $M_{(X)}$ - average of the plots with $X$ BEU size; $V_{(X)}$ - variance among plots of $X$ BEU size; $\mathrm{CV}_{(\mathrm{X})}$ coefficient of variation (in \%) among plots of $X$ BEU size; and $\mathrm{VU}_{(\mathrm{X})}$ - variance per BEU among the plots of $X$ BEU size $\left[\mathrm{VU}_{(\mathrm{x})}=\mathrm{V}_{(\mathrm{x})} / \mathrm{X}^{2}\right]$.

The parameters V1 (variance per BEU among the plots of a BEU size), b (index of heterogeneity), and the coefficient of determination ( $\mathrm{r}^{2}$ ) of the function $\mathrm{VU}_{(\mathrm{x})}=\mathrm{V} 1 / \mathrm{X}^{\mathrm{b}}$ of Smith (1938) were estimated. These parameters were estimated by logarithmic transformation and linearization of the function $\mathrm{VU}_{(\mathrm{X})}=\mathrm{V} 1 / \mathrm{X}^{\mathrm{b}}$, i.e., $\log \mathrm{VU}_{(\mathrm{x})}=\log \mathrm{V} 1-\mathrm{b} \log \mathrm{X}$, whose estimation was weighted by the degrees of freedom (DF = n -1), associated with each plot size, as applied by Sousa et al. (2016).

For each of the five compositions of sowing densities, 176 scenarios were planned formed by combinations of $i$ treatments ( $i=5,10,15$, and 20 ), $r$ repetitions ( $r=3,4,5$, and 6), and d differences between treatment averages to be detected as significant at 0.05 probability, expressed as a percentage of the overall average of the experiment, that is, in precision levels [ $\mathrm{d}=10$ (highest precision), $12,14,16,18$, $20,22,24,26,28$, and $30 \%$ (lowest precision)]. Subsequently, for the single crop composition of showy rattlebox ( $100 \%$ of CS ) the scenarios for $i=25$ and 30 and $r=7,8,9$, and 10 were added, totaling 528 scenarios for this composition. In addition, for these 528 scenarios the experiment size was calculated.

For each scenario, the optimal plot size (Xo), in number of BEU, was calculated using the expression

$$
X o=\sqrt[b]{\frac{2\left(\mathrm{t}_{1}+\mathrm{t}_{2}\right)^{2} \mathrm{CV}^{2}}{\mathrm{rd}^{2}}}(\text { Hatheway, 1961) }
$$

In this expression $b$ is the estimate of the soil heterogeneity index (in this study, for each composition, the average of $b$ from the three uniformity trials was considered); $\mathrm{t}_{1}$ is the
critical value of Student $t$-distribution for the significance level of the test (type I error) of $\alpha=5 \%$ (two-sided test at $5 \%$ ), with DF degrees of freedom; $t_{2}$ is the critical value of Student t -distribution, corresponding to 2(1-P) (two-sided test), where $P$ is the probability of obtaining a significant result, that is, the power of the test ( $P=0.80$, in this study), with DF degrees of freedom; CV is the estimate of the coefficient of variation among the plots of a BEU size (in this study, for each composition, the average CV of the three uniformity trials was considered), in percent; $r$ is the number of repetitions; and $d$ is the difference between treatment averages to be detected as significant at 0.05 probability, expressed as a percentage of the overall average of the experiment (precision). The degrees of freedom (DF) for obtaining the critical values (tabulated) of Student t-distribution were obtained by the expression DF = (i) $(r-1)$, where $i$ is the number of treatments and $r$ is the number of repetitions. The values of $t_{1}$ and $t_{2}$ were obtained with the Microsoft Office Excel ${ }^{\circledR}$ application, using the functions $\mathrm{t}_{1}=\operatorname{INVT}(0.05 ; \mathrm{DF})$ and $\mathrm{t}_{2}=\operatorname{INVT}(0.40 ; \mathrm{DF})$, respectively. The statistical analyses were performed with the help of Microsoft Office Excel ${ }^{\circledR}$ application.

## Results and Discussion

In the 15 uniformity trials, formed by compositions of sowing densities of sorghum (S. bicolor (L.) Moench) cultivar Nutribem (S) and showy rattlebox (C. spectabilis Roth.) (CS), the fresh matter (FM) productivity ranged between 2,174 and $4,016 \mathrm{~g} \mathrm{~m}^{-2}$, i.e., 21.74 and $40.16 \mathrm{Mg} \mathrm{ha}^{-1}$, respectively (Table 1).

The average of FM of the three intercrop compositions $\left(3,413 \mathrm{~g} \mathrm{~m}^{-2}\right)$ did not differ from the average of the sorghum single crop $\left(3,158 \mathrm{~g} \mathrm{~m}^{-2} ; \mathrm{t}=0.905135 ; \mathrm{p}\right.$-value $=0.386682$; with 10 degrees of freedom) and was higher than the average of the showy rattlebox single crop $\left(2,271 \mathrm{~g} \mathrm{~m}^{-2} ; \mathrm{t}=4.042117\right.$; $p$-value $=0.002353$; with 10 degrees of freedom). Among the single crops the FM of sorghum was higher than that of showy rattlebox ( $\mathrm{t}=7.114031$; p -value $=0.002063$; with 4 degrees of freedom).

For sorghum and showy rattlebox crops, 31.9 and 16.5 $\mathrm{Mg} \mathrm{ha}{ }^{-1}$ of FM were obtained by Torres et al. (2014), 25.74 and $33.9 \mathrm{Mg} \mathrm{ha}^{-1}$ by Passos et al. (2017), and 38.00 and 17.05 Mg ha ${ }^{-1}$ by Santos et al. (2020), respectively. Therefore, the superior FM ratio of sorghum, obtained in this study, was

Table 1. Planned plot size ( $X=X_{R} \times X_{C}$ ), in basic experimental units (BEU), with $X_{R}$ BEU adjacent in the row and $X_{C}$ BEU adjacent in the column; number of plots with X BEU size $(n=36 / X)$; average of the plots with X BEU size $\left[M_{(x)}\right]$, in $g$; and coefficient of variation (in \%) among plots of $X$ BEU size $\left[C V_{(x)}\right]$. Fresh matter productivity data at sowing densities of sorghum (Sorghum bicolor (L.) Moench) (S) and showy rattlebox (Crotalaria spectabilis Roth.) (CS).

| $E^{(1)}$ | $\mathrm{X}_{\mathrm{R}}$ | $\mathrm{X}_{\mathrm{c}}$ | X | n | 100\% of S |  | 75\% of S + 25\% of CS |  | 50\% of S + 50\% of CS |  | 25\% of S + 75\% of CS |  | 100\% of CS |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | $\mathrm{M}_{(\mathrm{X})}$ | $\mathrm{CV}_{(\mathrm{X})}$ | M(x) | CV(X) | $\mathrm{M}_{(\mathrm{X})}$ | CV ${ }_{(x)}$ | $\mathrm{M}_{(\mathrm{X})}$ | $\mathrm{CV}_{(\mathrm{x})}$ | $\mathrm{M}_{(\mathrm{X})}$ | CV(X) |
| 1 | 1 | 1 | 1 | 36 | 3,044 | 18.08 | 3,497 | 22.47 | 3,077 | 27.26 | 2,604 | 37.28 | 2,174 | 31.09 |
| 1 | 1 | 2 | 2 | 18 | 6,088 | 15.51 | 6,993 | 18.55 | 6,154 | 20.33 | 5,207 | 27.93 | 4,348 | 17.95 |
| 1 | 1 | 3 | 3 | 12 | 9,131 | 12.71 | 10,490 | 10.16 | 9,231 | 20.88 | 7,811 | 24.51 | 6,523 | 21.10 |
| 1 | 1 | 6 | 6 | 6 | 18,263 | 8.63 | 20,980 | 9.07 | 18,462 | 7.85 | 15,622 | 18.95 | 13,045 | 10.70 |
| 1 | 2 | 1 | 2 | 18 | 6,088 | 16.16 | 6,993 | 20.25 | 6,154 | 25.04 | 5,207 | 25.16 | 4,348 | 27.69 |
| 1 | 2 | 2 | 4 | 9 | 12,175 | 13.84 | 13,987 | 17.20 | 12,308 | 18.82 | 10,415 | 15.57 | 8,697 | 15.15 |
| 1 | 2 | 3 | 6 | 6 | 18,263 | 12.28 | 20,980 | 8.57 | 18,462 | 19.69 | 15,622 | 13.30 | 13,045 | 19.18 |
| 1 | 2 | 6 | 12 | 3 | 36,526 | 8.14 | 41,961 | 8.42 | 36,923 | 4.00 | 31,244 | 7.25 | 26,091 | 11.49 |
| 1 | 3 | 1 | 3 | 12 | 9,131 | 9.73 | 10,490 | 18.43 | 9,231 | 23.93 | 7,811 | 24.88 | 6,523 | 26.38 |
| 1 | 3 | 2 | 6 | 6 | 18,263 | 6.65 | 20,980 | 17.46 | 18,462 | 18.16 | 15,622 | 13.46 | 13,045 | 15.37 |
| 1 | 3 | 3 | 9 | 4 | 27,394 | 6.86 | 31,471 | 10.20 | 27,693 | 19.78 | 23,433 | 11.59 | 19,568 | 19.64 |
| 1 | 3 | 6 | 18 | 2 | 54,789 | 3.08 | 62,941 | 10.66 | 55,385 | 7.17 | 46,866 | 3.44 | 39,136 | 12.30 |
| 1 | 6 | 1 | 6 | 6 | 18,263 | 5.50 | 20,980 | 15.51 | 18,462 | 22.69 | 15,622 | 17.12 | 13,045 | 24.56 |
| 1 | 6 | 2 | 12 | 3 | 36,526 | 5.18 | 41,961 | 15.70 | 36,923 | 18.86 | 31,244 | 6.13 | 26,091 | 11.50 |
| 1 | 6 | 3 | 18 | 2 | 54,789 | 5.33 | 62,941 | 0.92 | 55,385 | 23.10 | 46,866 | 13.77 | 39,136 | 19.83 |
| 2 | 1 | 1 | 1 | 36 | 3,321 | 19.13 | 3,616 | 18.54 | 2,966 | 23.50 | 3,324 | 29.78 | 2,183 | 26.61 |
| 2 | 1 | 2 | 2 | 18 | 6,643 | 10.35 | 7,231 | 15.69 | 5,933 | 17.12 | 6,648 | 20.78 | 4,365 | 22.04 |
| 2 | 1 | 3 | 3 | 12 | 9,964 | 10.18 | 10,847 | 11.40 | 8,899 | 16.57 | 9,972 | 15.80 | 6,548 | 16.24 |
| 2 | 1 | 6 | 6 | 6 | 19,928 | 6.70 | 21,693 | 11.51 | 17,798 | 9.29 | 19,943 | 14.79 | 13,096 | 14.04 |
| 2 | 2 | 1 | 2 | 18 | 6,643 | 16.26 | 7,231 | 14.51 | 5,933 | 17.26 | 6,648 | 25.88 | 4,365 | 20.60 |
| 2 | 2 | 2 | 4 | 9 | 13,285 | 8.00 | 14,462 | 13.84 | 11,865 | 15.27 | 13,295 | 18.89 | 8,730 | 16.34 |
| 2 | 2 | 3 | 6 | 6 | 19,928 | 8.80 | 21,693 | 9.55 | 17,798 | 15.62 | 19,943 | 14.35 | 13,096 | 10.91 |
| 2 | 2 | 6 | 12 | 3 | 39,855 | 5.38 | 43,386 | 10.23 | 35,596 | 6.62 | 39,886 | 15.30 | 26,191 | 9.15 |
| 2 | 3 | 1 | 3 | 12 | 9,964 | 13.61 | 10,847 | 12.91 | 8,899 | 16.47 | 9,972 | 23.49 | 6,548 | 17.90 |
| 2 | 3 | 2 | 6 | 6 | 19,928 | 7.13 | 21,693 | 11.46 | 17,798 | 13.79 | 19,943 | 17.23 | 13,096 | 14.15 |
| 2 | 3 | 3 | 9 | 4 | 29,892 | 7.13 | 32,540 | 2.47 | 26,697 | 14.56 | 29,915 | 11.33 | 19,644 | 10.44 |
| 2 | 3 | 6 | 18 | 2 | 59,783 | 5.48 | 65,080 | 2.25 | 53,394 | 4.28 | 59,829 | 13.21 | 39,287 | 11.02 |
| 2 | 6 | 1 | 6 | 6 | 19,928 | 11.26 | 21,693 | 11.07 | 17,798 | 13.55 | 19,943 | 21.66 | 13,096 | 15.50 |
| 2 | 6 | 2 | 12 | 3 | 39,855 | 6.23 | 43,386 | 11.32 | 35,596 | 13.63 | 39,886 | 14.94 | 26,191 | 12.14 |
| 2 | 6 | 3 | 18 | 2 | 59,783 | 5.01 | 65,080 | 0.76 | 53,394 | 16.57 | 59,829 | 4.24 | 39,287 | 6.29 |

Continuation of Table 1

| $E^{(1)}$ | $\mathrm{X}_{\mathrm{R}}$ | $\mathrm{X}_{\mathrm{c}}$ | X | n | 100\% of S |  | 75\% of S + 25\% of CS |  | 50\% of S + 50\% of CS |  | 25\% of S + 75\% of CS |  | 100\% of CS |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | M(X) | $\mathrm{CV}_{(\mathrm{x})}$ | $\mathrm{M}(\mathrm{X})$ | $\mathrm{CV}_{(\mathrm{X})}$ | M(x) | CV(X) | $\mathrm{M}(\mathrm{X})$ | $\mathrm{CV}_{(\mathrm{X})}$ | $\mathrm{M}_{(\mathrm{X})}$ | $\mathrm{CV}_{(\mathrm{x})}$ |
| 3 | 1 | 1 | 1 | 36 | 3,109 | 20.18 | 3,959 | 21.99 | 4,016 | 21.79 | 3,661 | 26.25 | 2,455 | 30.55 |
| 3 | 1 | 2 | 2 | 18 | 6,218 | 15.68 | 7,918 | 18.31 | 8,031 | 15.43 | 7,321 | 21.99 | 4,911 | 22.46 |
| 3 | 1 | 3 | 3 | 12 | 9,326 | 12.82 | 11,877 | 14.45 | 12,047 | 10.59 | 10,982 | 21.23 | 7,366 | 21.57 |
| 3 | 1 | 6 | 6 | 6 | 18,653 | 11.14 | 23,753 | 11.10 | 24,094 | 6.57 | 21,964 | 14.57 | 14,733 | 16.13 |
| 3 | 2 | 1 | 2 | 18 | 6,218 | 17.92 | 7,918 | 16.13 | 8,031 | 16.45 | 7,321 | 20.53 | 4,911 | 26.39 |
| 3 | 2 | 2 | 4 | 9 | 12,435 | 14.47 | 15,836 | 12.48 | 16,062 | 10.43 | 14,642 | 18.07 | 9,822 | 18.29 |
| 3 | 2 | 3 | 6 | 6 | 18,653 | 12.45 | 23,753 | 9.82 | 24,094 | 7.75 | 21,964 | 18.25 | 14,733 | 18.81 |
| 3 | 2 | 6 | 12 | 3 | 37,306 | 12.20 | 47,507 | 6.89 | 48,187 | 6.90 | 43,927 | 11.62 | 29,465 | 12.94 |
| 3 | 3 | 1 | 3 | 12 | 9,326 | 14.80 | 11,877 | 15.01 | 12,047 | 11.76 | 10,982 | 14.34 | 7,366 | 19.75 |
| 3 | 3 | 2 | 6 | 6 | 18,653 | 12.58 | 23,753 | 13.80 | 24,094 | 5.07 | 21,964 | 9.76 | 14,733 | 13.52 |
| 3 | 3 | 3 | 9 | 4 | 27,979 | 9.60 | 35,630 | 11.07 | 36,141 | 5.67 | 32,945 | 12.71 | 22,099 | 14.03 |
| 3 | 3 | 6 | 18 | 2 | 55,959 | 10.68 | 71,260 | 4.19 | 72,281 | 3.47 | 65,891 | 0.95 | 44,198 | 11.79 |
| 3 | 6 | 1 | 6 | 6 | 18,653 | 12.09 | 23,753 | 9.48 | 24,094 | 7.10 | 21,964 | 6.07 | 14,733 | 13.54 |
| 3 | 6 | 2 | 12 | 3 | 37,306 | 10.48 | 47,507 | 7.39 | 48,187 | 4.62 | 43,927 | 2.80 | 29,465 | 9.62 |
| 3 | 6 | 3 | 18 | 2 | 55,959 | 3.66 | 71,260 | 3.14 | 72,281 | 4.01 | 65,891 | 1.39 | 44,198 | 7.70 |

${ }^{(1)}$ Each uniformity trial of size $6.0 \times 6.0 \mathrm{~m}\left(36.0 \mathrm{~m}^{2}\right)$ was divided into 36 BEU of $1.0 \times 1.0 \mathrm{~m}\left(1.0 \mathrm{~m}^{2}\right)$, forming a matrix of six rows and six columns.
also observed by Torres et al. (2014) and Santos et al. (2020). On the other hand, Passos et al. (2017) found FM superiority of showy rattlebox. Also, Pereira et al. (2012) obtained $39.10 \mathrm{Mg} \mathrm{ha}^{-1}$ of FM of showy rattlebox. The fact that these studies were conducted under different environmental conditions, cultural management, and evaluation times makes comparisons with the results of this study difficult.

The coefficient of variation (CV) of FM, obtained among the 36 BEU in each of the 15 uniformity trials, ranged from 18.08 to $37.28 \%$, with an average of $24.97 \%$ (Table 1). The averages of CV, from the three trials of each composition were $19.13,21.00,24.18,31.10$, and $29.42 \%$, for the compositions of $100 \%$ of $S ; 75 \%$ of $S+25 \%$ of CS; $50 \%$ of $S+50 \%$ of CS; $25 \%$ of $S+75 \%$ of CS; and $100 \%$ of CS, respectively. Most of these coefficients are considered high according to Pimentel-Gomes (2009) classification, i.e., they are in the 20.0 to $30.0 \%$ range. In experiments with sorghum, showy rattlebox, and other species, CV of $39.78 \%$ (Pereira et al., 2012), $12.46 \%$ (Torres et al., 2014), $37.73 \%$ (Passos et al., 2017), and $16.33 \%$ (Santos et al., 2020) were obtained, therefore similar to those obtained in these 15 uniformity trials.

Smith (1938) heterogeneity index (b) ranged from 0.6042 to 1.2571 (Figure 1). The averages of $b$, from the three trials for each composition were $0.8179,0.8514,0.8350,0.9899$, and 0.7345 for the compositions of $100 \%$ of $\mathrm{S}, 75 \%$ of $\mathrm{S}+$ $25 \%$ of CS, $50 \%$ of $S+50 \%$ of CS, $25 \%$ of $S+75 \%$ of CS, and $100 \%$ of CS, respectively. Values of $b$ close to unity were also obtained in grain sorghum (Lopes et al., 2005; Brum et al., 2008), sunflower (Sousa et al., 2016), forage palm (Guimarães et al., 2020), and in species with potential for ground cover, such as: buckwheat (Cargnelutti Filho et al., 2020a); black oat + vetch (Cargnelutti Filho et al., 2020b); millet + slender leaf rattlebox (Cargnelutti Filho et al., 2021a); millet + showy rattlebox (Cargnelutti Filho et al., 2021b); and black oat + common vetch + forage turnip (Cargnelutti Filho et al., 2022).

When $b>0.7$, it is recommended to increase the plot size, when $b<0.2$, one should increase the number of repetitions,
and in cases of $0.2 \leq b \leq 0.7$ it is appropriate to investigate the best combination of plot size and number of repetitions (Lin \& Binns, 1986). Therefore, the high values of $b$ (Figure 1) indicate that sorghum and showy rattlebox experiments, in single or intercropping, should prioritize the use of larger plots.

With increasing the planned plot size ( X ), there was a decrease in the coefficient of variation $\left[\mathrm{CV}_{(x)}\right]$ and the variance per BEU among plots $\left[\mathrm{VU}_{(\mathrm{x})}\right]$ (Table 1 and Figure 1), which means improvement in experimental precision. Sharp decreases in $\mathrm{VU}_{(\mathrm{X})}$ were observed with plots up to four BEU ( $4 \mathrm{~m}^{2}$ ), intermediate between four and ten BEU, and a stabilizing trend with plots larger than ten BEU $\left(10 \mathrm{~m}^{2}\right)$. Thus, it is suggested to use plots up to $10 \mathrm{~m}^{2}$, because the gain in experimental precision (decrease of $\mathrm{VU}_{(\mathrm{x})}$ ), from ten BEU , was inexpressive. Similar pattern was observed in buckwheat (Cargnelutti Filho et al., 2020a); black oat + common vetch (Cargnelutti Filho et al., 2020b); millet + slender leaf rattlebox (Cargnelutti Filho et al., 2021a); millet + showy rattlebox (Cargnelutti Filho et al., 2021b); and black oat + common vetch + forage turnip (Cargnelutti Filho et al., 2022).

In the five compositions of S and CS sowing densities, it is observed that with fixed values of $i$ and $r$, Xo increased with increasing precision (d); with fixed values of $i$ and $d, X o$ decreased with increasing $r$; and with fixed values of $r$ and $d$, there was a decrease in Xo with increasing i (Figures $\underline{2}$ and 3). This pattern is in agreement with the results obtained by Cargnelutti Filho et al. (2020a, 2020b, 2021a, 2021b, 2022).

For fixed values of $i, r$, and $d$, the $100 \%$ of CS composition, with soil heterogeneity index $b=0.7345$ and $C V=29.42 \%$, showed larger plot sizes compared to the other compositions ( $100 \%$ of $\mathrm{S} ; 75 \%$ of $S+25 \%$ of CS; $50 \%$ of $S+50 \%$ of CS; and $25 \%$ of $S+75 \%$ of CS) (Figures $\underline{2}$ and $\underline{3}$ ). Therefore, the results of this composition can be used as a reference for defining the plot size and number of repetitions, in order to ensure sufficient experimental precision for experiments with sorghum and showy rattlebox, in single and intercropping.


Figure 1. Relationship between the variance per basic experimental unit (BEU) between $X$ BEU plot sizes $\left[V U_{(X)}=V_{(X)} / X^{2}\right]$ and the planned plot size ( X ), in BEU, and the parameter estimates of the function $\mathrm{VU}_{(\mathrm{X})}=\mathrm{V} 1 / \mathrm{X}^{\mathrm{b}}$ of $\underline{S m i t h}$ (1938). Fresh matter productivity data obtained in uniformity trials, with 36 BEU of $1.0 \mathrm{~m}^{2}$, formed by compositions of sowing densities of sorghum (Sorghum bicolor (L.) Moench) (S) and showy rattlebox (Crotalaria spectabilis Roth.) (CS).

In addition to the plot sizes, calculated for the combinations of $i, r$, and $d$ (Figures $\underline{2}$ and $\underline{3}$ ), numerous other scenarios can be simulated using the expression

$$
\mathrm{Xo}=\sqrt[b]{\frac{2\left(\mathrm{t}_{1}+\mathrm{t}_{2}\right)^{2} \mathrm{CV}^{2}}{\mathrm{rd}^{2}}}(\text { Hatheway, 1961) }
$$


$i$ treatments $(i=5,10,15$, and 20) and d precision levels ( $\mathrm{d}=10,12,14,16,18,20,22,24,26,28$, and $30 \%$ )
Figure 2. Optimal plot size, in $m^{2}$, for combinations of $i$ treatments ( $i=5,10,15$, and 20 ), $r$ repetitions ( $r=3,4,5$, and 6 ), and $d$ precision levels ( $\mathrm{d}=10,12,14,16,18,20,22,24,26,28$, and $30 \%$ ), for the fresh matter productivity in intercrops of sorghum (Sorghum bicolor (L.) Moench) and showy rattlebox (Crotalaria spectabilis Roth.).

$i$ treatments $(i=5,10,15$, and 20) and d precision levels $(d=10,12,14,16,18,20,22,24,26,28$, and $30 \%)$
Figure 3. Optimal plot size, in $\mathrm{m}^{2}$, for combinations of i treatments ( $i=5,10,15$, and 20 ), $r$ repetitions $(r=3,4,5$, and 6 ), and $d$ precision levels ( $d=10,12,14,16,18,20,22,24,26,28$, and $30 \%$ ), for fresh matter productivity in single crops of sorghum (Sorghum bicolor (L.) Moench) and showy rattlebox (Crotalaria spectabilis Roth.).
based on the average soil heterogeneity index (b) of the Smith (1938) function and the average coefficient of variation (CV) of FM, from the three trials of each composition. Thus, the following estimates would be used for the compositions: $100 \%$ of $S(b=0.8179 ; C V=19.13 \%), 75 \%$ of $S+25 \%$ of CS ( $b=0.8514 ; C V=21.00 \%$ ), $50 \%$ of $S+50 \%$ of $C S ~(b=0.8350 ;$ $C V=24.18 \%), 25 \%$ of $S+75 \%$ of $C S(b=0.9899 ; C V=31.10 \%)$, and $100 \%$ of CS ( $b=0.7345$; CV = 29.42\%) (Table 2).

As an example, to evaluate the FM of six treatments of the $100 \%$ of CS composition, with five repetitions and with $d=$ $24 \%$, one has: $b=0.7345 ;$ DF $=(6)(5-1)=24 ; \mathrm{t}_{1}=\operatorname{INVT}(0.05 ; 24)$ $=2.063898547 ; \mathrm{t}_{2}=\operatorname{INVT}(0.40 ; 24)=0.856855458 ; \mathrm{CV}=$ $29.42 \% ; r=5 ; d=24 \%$. Soon,
$X o=\sqrt[0.7345]{\frac{2(2.063898547+0.856855458)^{2} 29.45^{2}}{5 \times 24^{2}}}=9.26 \mathrm{BEU}$.

Therefore, using the criterion of rounding up to the next whole number, the plot size for this example would be $10 \mathrm{~m}^{2}$. Following this example, 528 scenarios were generated and the optimal plot size and experiment size calculated to serve as a reference for planning future experiments (Table 2).

This size of $10 \mathrm{~m}^{2}$ is relatively larger than those established for grain sorghum that were $3.2 \mathrm{~m}^{2}$ (Lopes et al., 2005) and $0.5 \mathrm{~m}^{2}$ (Brum et al., 2008), equal to the $10 \mathrm{~m}^{2}$ established for the single and intercropped crops of black oat + common vetch (Cargnelutti Filho et al, 2020b), millet + slender leaf rattlebox (Cargnelutti Filho et al., 2021a), and millet + showy rattlebox (Cargnelutti Filho et al., 2021b). Additionally, this size of $10 \mathrm{~m}^{2}$ is relatively smaller than those used in experiments with sorghum and showy rattlebox, along with other ground cover species, by Pereira et al. (2012), Torres et al. (2014), and Passos et al. (2017), which ranged between 37.5 and $63.0 \mathrm{~m}^{2}$.

Table 2. Optimal plot and experiment sizes, in $\mathrm{m}^{2}$, for combinations of i treatments, r repetitions, and d precision levels (\%), for fresh matter productivity of single showy rattlebox (Crotalaria spectabilis Roth.), based on the soil heterogeneity index $b=$ 0.7345 and CV $=29.42 \%$.


## Conclusions

In experiments to evaluate the fresh matter productivity of sorghum and showy rattlebox, in single or intercropped cultivation, with 5 to 30 treatments and with five repetitions, plots of $10.0 \mathrm{~m}^{2}$ of useful area are sufficient for differences between treatments of $24 \%$ of the overall average of the experiment to be considered significant at 0.05 probability.

## Acknowledgements

To the Conselho Nacional de Desenvolvimento Científico e Tecnológico (CNPq - Process 304652/2017-2), the Coordenação de Aperfeiçoamento de Pessoal de Nível Superior (CAPES), and the Fundação de Amparo à Pesquisa do Estado do Rio Grande do Sul (FAPERGS) for granting scholarships to the authors. To the scholarship students and volunteers for helping in data collection.

## Compliance with Ethical Standards

Author contributions: Conceptualization: ACF; Data curation: ACF, IMMN, VST, LFO, VMO; Formal analysis: ACF; Funding acquisition: ACF; Investigation: ACF, IMMN, VST, LFO, VMO; Methodology: ACF; Project administration: ACF; Resources: ACF; Software: ACF; Supervision: ACF; Validation: ACF; Visualization: ACF; Writing - original draft: ACF; Writing review \& editing: ACF, IMMN, VST, LFO, VMO.

Conflict of interest: We have no conflict of interest (professional or financial) that may influence the article.

Financing source: The Conselho Nacional de Desenvolvimento Científico e Tecnológico (CNPq) - Process 304652/2017-2, the Coordenação de Aperfeiçoamento de Pessoal de Nível Superior (CAPES) - Finance Code 001, and the Fundação de Amparo à Pesquisa do Estado do Rio Grande do Sul (FAPERGS).

## Literature Cited

Alvares, C.A.; Stape, J.L.; Sentelhas, P.C.; Gonçalves, J.L.M.; Sparovek, G. Köppen's climate classification map for Brazil. Meteorologische Zeitschrift, v.22, n.6, p.711-728, 2013. https:// doi.org/10.1127/0941-2948/2013/0507.
Brum, B.; Lopes, S.J.; Storck, L.; Santos, V.J.; Benz, V.; Lovato, C. Tamanho ótimo de parcela para ensaios com sorgo granífero em duas épocas de semeadura. Ciência Rural, v.38, n.2, p.315-320, 2008. https://doi.org/10.1590/S0103-84782008000200003.

Cargnelutti Filho, A.; Neu, I.M.M.; Loregian, M.V.; Bubans, V.E.; Somavilla, F.M.; Dumke, G.E. Experimental dimensions and precision in trials with millet and slender leaf rattlebox. Revista Ciência Agronômica, v.52, n.3, e20207434, 2021a. https://doi. org/10.5935/1806-6690.20210045.
Cargnelutti Filho, A.; Neu, I.M.M.; Souza, J.M.; Pezzini, R.V.; Dumke, G.E.; Somavilla, F.M. Plot size, number of treatments and replicates and experimental precision in buckwheat. Revista Caatinga, v.33, n.4, p.1131-1139, 2020a. https://dx.doi. org/10.1590/1983-21252020v33n428rc.
Cargnelutti Filho, A.; Silveira, D.L.; Loregian, M.V.; Osmari, L.F.; Ortiz, V.M. Experimental design and precision in trials with black oat, common vetch, and forage turnip intercropping. Revista Brasileira de Ciências Agrárias, v.17, n.2, e129, 2022. https://doi. org/10.5039/agraria.v17i2a129.
Cargnelutti Filho, A.; Souza, J.M.; Pezzini, R.V.; Neu, I.M.M.; Silveira, D.L.; Procedi, A. Optimal plot size for experiments with black oats and the common vetch. Ciência Rural, v.50, n.3, p.e20190123, 2020b. https://dx.doi.org/10.1590/0103-8478cr20190123.
Cargnelutti Filho, A.; Souza, J.M.; Silveira, D.L.; Costa, S.L.; Osmari, B.F.; Osmari, L.F. Experimental dimensions and precision in trials with millet and showy rattlebox. Revista Brasileira de Ciências Agrárias, v.16, n.3, e8686, 2021b. https://doi.org/10.5039/agraria.v16i3a8686.

Donato, S.L.R.; Silva, J.A.; Guimarães, B.V.C.; Silva, S.O. Experimental planning for the evaluation of phenotipic descriptors in banana. Revista Brasileira de Fruticultura, v.40, n.5, e962, 2018. https:// doi.org/10.1590/0100-29452018962.

Guimarães, B.V.C.; Donato, S.L.R.; Aspiazú, I.; Azevedo, A.M.; Carvalho, A.J. Optimal plot size for experimental trials with Opuntia cactus pear. Acta Scientiarum. Technology, v.42, e42579, 2020. https://doi.org/10.4025/actascitechnol.v42i1.42579.

Hatheway, W.H. Convenient plot size. Agronomy Journal, v.53, n.4, p.279-280, 1961. https://doi.org/10.2134/agronj1961.0002196 2005300040025x.
Lin, C.S.; Binns, M.R. Relative efficiency of two randomized block designs having different plot sizes and numbers of replications and of plots per block. Agronomy Journal, v.78, n.3, p.531-534, 1986. https://doi.org/10.2134/agronj1986.0002196200780003 0029x.
Lopes, S.J.; Storck, L.; Lúcio, A.D.; Lorentz, L.H.; Lovato, C.; Dias, V.O. Tamanho de parcela para produtividade de grãos de sorgo granífero em diferentes densidades de plantas. Pesquisa Agropecuária Brasileira, v.40, n.6, p.525-530, 2005. https://doi. org/10.1590/S0100-204X2005000600001.
Oliveira, J.R.; Santana, W.R.; Santos, M.N.; Schmildt, E.R. Determination of the optimum plot size for tomato seedlings. Revista Ceres, v.68, n.2, p.126-134, 2021. https://doi. org/10.1590/0034-737X202168020006.
Passos, A.M.A.; Aker, A.M.; Costa, R.S.C.; Santos, F.C.; Leite, V.P.D.; Marcolan, A.L. Effect of cover crops on physico-chemical attributes of soil in a short-term experiment in the southwestern Amazon region. African Journal of Agricultural Research, v.12, n.47, p.3339-3347, 2017. https://doi.org/10.5897/ AJAR2017.12800.
Pereira, G.A.M.; Silva, D.V.; Braga, R.R.; Carvalho, F.P.; Ferreira, E.A.; Santos, J.B. Fitomassa de adubos verdes e cobertura do solo na região do Alto Vale do Jequitinhonha, Minas Gerais. Revista Agro@mbiente On-line, v.6, n.2, p.110-116, 2012. https:// dx.doi.org/10.18227/1982-8470ragro.v6i2.696.

Pimentel-Gomes, F. Curso de estatística experimental. Piracicaba: FEALQ, 2009. 451p.
Santos, H.G.; Jacomine, P.K.T.; Anjos, L.H.C.; Oliveira, V.A.; Lumbreras, J.F.; Coelho, M.R.; Almeida, J.A.; Araújo Filho, J.C.; Oliveira, J.B.; Cunha, T.J.F. Sistema Brasileiro de Classificação de Solos. Brasília: Embrapa, 2018. 356p.
Santos, V.F.; Silva, L.F.; Araújo Neto, J.R.; Silva, V.P.; Rocha, A.T.; Santos, G.M. Produção de fitomassa por plantas de cobertura no Agreste Meridional de Pernambuco. Ciência Agrícola, v.18, n.3, p.31-35, 2020. https://doi.org/10.28998/rca.v18i3.9449.

Smith, H.F. An empirical law describing heterogeneity in the yields of agricultural crops. Journal of Agricultural Science, v.28, n.1, p.1-23, 1938. https://doi.org/10.1017/S0021859600050516.

Sousa, R.P.; Silva, P.S.L.; Assis, J.P. Tamanho e forma de parcelas para experimentos com girassol. Revista Ciência Agronômica, v.47, n.4, p.683-690, 2016. https://doi.org/10.5935/18066690.20160082 .

Torres, J.L.R.; Cunha, M.A.; Pereira, M.G.; Vieira, D.M.S. Cultivo de feijão e milho em sucessão a plantas de cobertura. Revista Caatinga, v.27, n.4, p.117-125, 2014. https://periodicos.ufersa. edu.br/index.php/caatinga/article/view/3213/pdf 178. 21 Sep. 2021.


[^0]:    * Alberto Cargnelutti Filho - E-mail: alberto.cargnelutti.filho@gmail.com (Corresponding author)

    Associate Editor: Mario de Andrade Lira Júnior

